Iterative sparsity score for feature selection and its extension for multimodal data

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\textbf{A B S T R A C T}

As a key dimensionality reduction technique in pattern recognition, feature selection has been widely used in information retrieval, text classification and genetic data analysis. In recent years, structural information contained in samples for guiding feature selection has become a new hot spot in machine learning field. Although tremendous feature selection methods have been developed, less important features are still used to construct the structure in those conventional structure based feature selection approaches. In this paper, we propose a new filter-type feature selection method called iterative sparsity score, which is independent of any learning algorithm. The proposed method can preserve the structural information by sparse representation, which can be efficiently solved by a \(\ell_1\)-norm minimization problem. To exclude data noise, at one time we discard last \(m\) features and iteratively optimize the \(\ell_1\)-norm minimization problem. We perform clustering and classification experiments on numerous benchmark datasets. Furthermore, its extension for multimodal data is also developed. We adopt the multi-modality Alzheimer’s disease data for classification to evaluate the extended method. The experimental results show the effectiveness of our proposed methods compared with several popular feature selection approaches.

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1. Introduction

With the rapid development of technology, big data have emerged with large dimensions or huge numbers. For example, high resolution face pictures include a lot of information with high dimensions, but at the same time the high dimensions limit the utilization in practical applications. One 3-D magnetic resonance image contains tremendous features, while the number of samples is very small in medical image analysis [1–3]. For biomedical research, thousands of genes are in dozens of samples of microarray databases [4]. Those applications are typical small sample size problems, which mean there is small number of samples with high dimensionality in those data. It is very difficult to use machine learning methods for learning on those data. Directly adopting the high dimensional data for classification or clustering is time-consuming [5,6]. The features extracted from raw data always contain noises, which affect its true distribution. And those noisy features will reduce the performance of learning.

Dimensionality reduction which can be divided into features selection and feature extraction is used for reducing the number of random variables under consideration [7,8] in machine learning and pattern recognition fields [9–12]. Feature selection methods [13–15] try to find a subset of features and feature extraction [16,17] approaches transform the data in the high-dimensional space to a new feature space with fewer dimensions. Filter [18] and wrapper [19] strategies are widely used in feature selection approaches. Filter based methods evaluate features via intrinsic properties (e.g., information gain) of the data. Wrapper techniques select features on which the learning process can achieve the predefined goal. In our paper, we currently focus on filter-type feature selection methods.

There are several popular filter-type feature selection methods, such as variance (Var) [20], Fisher Score (FS) [20], Laplacian Score (LS) [21], and Sparsity Score (SS) [22]. Among those filter-type feature selection approaches, Sparsity Score (SS) based on \(\ell_1\)-norm minimization can preserve the structure of a predefined graph. However, SS involves all the features constructing the predefined graph. Obviously, the noisy features will embed irrelevant information into the graph. In this paper, we propose a novel iterative sparsity score method to solve the above problem. At a time, we discard last \(m\) features to construct the graph, and then iteratively...
solve the \( \ell_1 \)-norm minimization problem. The proposed method is compared with 4 popular filter-type feature selection approaches (including supervised and unsupervised). Besides, we also extend our proposed feature selection method to deal with multimodal problems. Experimental results on both clustering and multimodal classification demonstrate the effectiveness of our proposed algorithms.

The rest of the paper is organized as follows. The background is introduced and several typical filter-type feature selection methods are discussed in Section 2. In Section 3, we present the proposed iterative sparsity score feature selection method. Both clustering and classification experimental results are reported in Section 4. Section 5 gives the conclusion.

2. Related works

Assume we have a set of data \( X = \{x_1, x_2, \ldots, x_n\} \in \mathbb{R}^{d \times n} \), where \( n \) is the number of sample points and \( d \) is the feature dimension. \( x_i \in \mathbb{R}^d \) is the \( i \)th sample. The \( r \)th feature of the \( i \)th sample \( x_i \) is denoted as \( f_{ri} \), \( r = 1, \ldots, d \). Let \( \mu_r = \frac{1}{n} \sum_{i=1}^{n} f_{ri} \) represent the mean of the \( r \)th feature. If there is supervised information with the data, class labels of the data are given in \( [1, 2, \ldots, l] \), where \( l \) is the number of categories. \( f_r^i \) is the feature vector containing the \( r \)th feature, which belongs to the \( l \)th class. Let \( \mu_r^l \) denote the mean of class \( l \) corresponding to the \( r \)th feature, \( n_l \) denotes the number of data points belonging to the \( l \)th category.

Laplacian Score is obtained to reflect the locality preserving power of each feature, which is based on the assumption that, two data points from the same class should be close to each other. Laplacian Score seeks those features that respect the local geometric structure via a nearest neighbor graph. Let \( L_S \) denote the Laplacian Score of the \( r \)th feature, which should be minimized as follows [21]:

\[
L_S = \frac{\sum_{ij} (f_{ri} - f_{rj})^2 S_{ij}}{\sum_{ij} (f_{ri} - \mu_r)^2 D_{ij}}
\]

where \( D \) is a diagonal matrix and \( D_{ij} = \sum_j S_{ij} \), and \( S_{ij} \) is defined by the local relationship between sample points \( x_i \) and \( x_j \) as follows:

\[
S_{ij} = \begin{cases} 
1 & \text{if } x_i \text{ and } x_j \text{ are close} \\
0 & \text{otherwise}
\end{cases}
\]

Here, \( t \) is a fixed parameter in experiments and the term \( x_i \) and \( x_j \) are close means that \( x_i \) is among the \( k \) nearest neighbors of \( x_j \) or \( x_j \) is among the \( k \) nearest neighbors of \( x_i \).

Linear Discriminant Analysis (LDA) uses fisher criterion for dimensionality reduction, which also can be used for feature evaluation. Fisher Score assigns high scores to the features that can maximize the distance of data points of different classes while minimize the distance of data points of the same class. We denote the fisher score of the \( r \)th feature as \( F_S \) and the criteria could be maximized as follows [20]:

\[
F_S = \sum_{r=1}^{d} \frac{n_l (\mu_r^l - \mu_r)^2}{\sum_{r=1}^{d} (f_{ri} - \mu_r^l)^2}
\]

Sparsity score [22], a \( \ell_1 \) graph-preserving feature selection method is proposed based on this graph-preserving framework. After computing the sparse reconstructive weight matrix, the sparsity score \( S_S \) of the \( r \)th feature could be defined as follows:

\[
S_S = \frac{\sum_{i} (f_{ri} - \tilde{S}_{ij} f_{rj})^2}{\frac{1}{n} \sum_{i} (f_{ri} - \mu_r)^2}
\]

where \( \tilde{S}_{ij} \) is the entry of the sparse reconstruction weight matrix constructed using all data points. We will present the detail of this method in the following Section 3.3.

3. Iterative sparsity score feature selection

3.1. Sparse representation

Recently, sparse representation has been extensively applied in signal processing, pattern recognition and machine learning to solve many practical problems. For instance, in signal processing fields, sparse representation is proposed as an extension signal representation such as Fourier and Wavelet representation [23,24]. Sparse representation is adopted for target recognition, signal classification and reconstruction [25-27]. Classifier based on sparse representation [28] has achieved exciting recognition rate on some face data sets. Sparse representation is related with the famous feature selection method LASSO [29]. Given a sample vector \( x \in \mathbb{R}^d \), and a matrix \( X = [x_1, x_2, \ldots, x_n] \in \mathbb{R}^{d \times n} \) which contains the elements of an overcomplete dictionary in its columns. The purpose of sparse representation is to represent sample \( x \) using as fewer entries of \( X \) as possible. The objective function can be formulated as follows [30,31]:

\[
\min \| s \|_0 \quad \text{s.t.} \quad x = Xs
\]

\[
\min \| s \|_1 \quad \text{s.t.} \quad x = Xs
\]

where \( s \in \mathbb{R}^d \) is the coefficient vector, and \( \| s \|_0 \) is the pseudo-\( \ell_0 \) norm which is the number of non-zero components in \( s \). While \( \ell_0 \) is not convex and to find the optimal solution of Eq. (5) is NP-hard. The above problem can be transformed to \( \ell_1 \) and could be approximately solved by the following [28]

\[
\min \| s \|_1 \quad \text{s.t.} \quad x = Xs
\]

where \( \ell_1 \) is used to replace \( \ell_0 \). It has been shown that the solution of \( \ell_0 \) minimization problem is equal to the solution of \( \ell_1 \) minimization problem under some situations [32,33], Fig. 1 demonstrates that the \( \ell_1 \) norm minimization can find the sparse solution, but \( \ell_2 \) norm minimization cannot get the optimal sparse solution.

There have been so many works studying the equivalence of the \( \ell_0 \) and \( \ell_1 \) problem that the \( \ell_1 \) approximate strategy is more reliable than other methods. The Eq. (6) can be efficiently solved via standard linear programming [31].

In practical applications, because there are always some noises in data, the constraint \( x = Xs \) in Eq. (6) does not hold. Refer to [28], two robust extensions are proposed to handle this problem: (1) relax the constraint to \( \| x - Xs \| < \xi \), where \( \xi \) is an error tolerance; (2) replace \( X \) with \( [X, I] \), where \( I \) is an \( d \)-order identity matrix. We use the first strategy in this paper.

3.2. Sparse reconstructive weights

Recently, Qiao et al. [34] constructed a sparse reconstructive weight matrix based on a modified sparse representation framework, and explained why the matrix can help to find the most compact representation of data. Assume we have \( n \) training samples \( \{x_i\}_{i=1}^{n} \), where \( x_i \in \mathbb{R}^d \). Denote \( X = [x_1, x_2, \ldots, x_n] \in \mathbb{R}^{d \times n} \) as
data matrix. For each \( x_i \), we can obtain the sparse reconstructive weight vector \( s_i \) through the following modified \( \ell_1 \) minimization problem [34]:

\[
\begin{align*}
\text{min} & \quad ||s_i||_1 \\
\text{s.t.} & \quad x_i = Xs_i \\
\text{where} & \quad s_i = [s_{i,1}, \ldots, s_{i,i-1}, 0, s_{i,i+1}, \ldots, s_{i,n}]^T \text{ is an } n\text{-dimensional vector in which the } i\text{th element is equal to zero suggesting that } x_i \text{ is removed from } X. \text{The element } s_{i,j}(j \neq i) \text{ denotes the contribution of each } x_j \text{ to reconstruct } x_i; \quad t \in \mathbb{R}^n \text{ is a all ones vector. We find the sum-to-one constraint } 1 = t^Ts_i \text{ is linear, so the modified sparse representation problem can also be solved by standard linear programming.}
\end{align*}
\]

For each \( x_i, i = 1, 2, \ldots, n \), after obtaining the corresponding weight vector \( \tilde{s}_i \), the sparse reconstructive weight matrix can be defined as \( S = (\tilde{s}_i)_{n \times n} \) as follows:

\[
S = [\tilde{s}_1, \tilde{s}_2, \ldots, \tilde{s}_n]^T
\]

where \( \tilde{s}_i \) is the optimal solution of Eq. (7). It is worth noting that the weight matrix \( S \) not only reflects some intrinsic geometric properties of the data, but also preserves potential discriminant information even if no class labels are provided. The assumption is that the non-zero entries in \( \tilde{s}_i \) mostly indicate the samples from the same class, so that \( \tilde{s}_i \) can help to discriminate that class from the others.

As mentioned before, in many real-world problems, the constraint \( x_i = X \tilde{s}_i \) in Eq. (7) does not always hold. The two robust extensions in Section 3.1 can be used in the modified sparse representation to overcome the problem. The first extension is as follows:

\[
\begin{align*}
\text{min} & \quad ||s_i||_1 \\
\text{s.t.} & \quad ||x_i - Xs_i|| < \xi \\
\text{where} & \quad \xi \text{ is the error tolerance. As we can see, the optimal solution of Eq. (9) reflects some intrinsic geometric properties (e.g. invariant to translations and rotations) of the original data. The second extension is presented as follows:}
\end{align*}
\]

\[
\begin{align*}
\text{min} & \quad ||s_i^2 + t_i^2||_1 \\
\text{s.t.} & \quad \begin{bmatrix} x_i \\ 1 \end{bmatrix} = X \begin{bmatrix} t_i \\ 0 \end{bmatrix} \begin{bmatrix} s_i \\ 1 \end{bmatrix}
\end{align*}
\]

where \( t_i \) is a d-dimensional vector which is induced as a reconstructive compensation term. And \( \mathbf{0} \) is a d-dimensional vector of all zeros. The optimal solution of Eq. (9) is also invariant to translations, but the invariance to rotations and rescaling does not rigorously hold.

3.3. Sparsity score

Eq. (4) is the objective function of sparsity score. After several algebra operation, we can have the more compact format:

\[
SS_i = \frac{\sum_{i=1}^{n} (f_i - \sum_{j=1}^{n} f_{ij}^2)^2}{\frac{n}{d} \sum_{i=1}^{n} (f_i - \mu_d)^2} = \frac{f_i^2 (I - S^2 + S^TS)}{f_i^2 (I - \frac{1}{d} I)(I - S^S)}
\]

where \( S \) is the sparse reconstructive weight matrix via minimizing the modified \( \ell_1 \) problem Eq. (7). As we can see the numerator in Eq. (11), if \( f_{ij} \) can be well represented by other features, the value of the numerator will be small. At the same time, variance is considered in the denominator, in which \( f_i \) with big variance can

Algorithm 1 Iterative sparsity feature selection.

Input:
- The data set \( X \) with \( d \) features, selected feature number \( z \);

Output:
- \( z \) ranked feature list

1. repeat
2. Construct sparse \( \ell_1 \) graph for data \( X \)
3. Compute Sparsity Score for the features in \( X \)
4. Rank the features according to their sparsity scores in ascending order
5. Discard the last \( m \) features and update data \( X \) consisting of only the rest features
6. until \( t \geq T \)

result in small value of the sparsity score. Thus the features with high values can best respect the predefined \( \ell_1 \) graph structure (i.e. with small reconstruction error) as well as large variance.

3.4. Iterative sparsity score

Sparsity score adopts the \( \ell_1 \) graph constructed via the whole data set, in which the features with small scores are still included. In this section, we are going to present the improved sparsity score method called iterative sparsity score. The proposed method can iteratively update the sparse \( \ell_1 \) graph for evaluating the importance of features by its sparsity preserving ability. The key idea of iterative sparsity score is to gradually improve the sparse graph by discarding the least relevant features at each iteration.

Specifically, the algorithm finds the initial \( \ell_1 \) graph structure from the whole dataset. After calculating the sparsity score with the initial \( \ell_1 \) graph, we can rank the features. Then those features which respect the sparse structure are kept, while we abandon those features with small sparsity scores. In the next iterative step, the sparse \( \ell_1 \) graph is obtained via the reserved features. Repeat the above procedure, finally the optimal structural information in the data would be unearthed.

Given data \( X = [x_1, x_2, \ldots, x_n] \in \mathbb{R}^{d \times n} \), where \( x_i \in \mathbb{R}^d \) is a d-dimensional sample point. Let \( SS_i \) and \( G_i \) denote the sparsity score of the \( i \)th feature and the \( \ell_1 \) graph structure in the \( i \)th iteration, respectively. We first compute the sparse \( \ell_1 \) graph \( G_i \) by Eq. (9). Then calculate the sparsity score corresponding to the \( d \) features via Eq. (4). Discard the \( m \) features with the last \( m \) minimum sparsity score. Construct the next sparse \( \ell_1 \) graph with the rest of the \( d - m \) features. Repeat the iteration, until \( t \geq T \). Here \( T = \lceil \frac{n}{m} \rceil \) is the maximum iteration and \( z \) is the number of features reserved. The detail of our proposed method is shown in Algorithm 1.

It is worth noting that not only sparsity score can be extended to the iterative version, other feature selection based on score criterion also can have their iterative versions.

3.5. Multimodal iterative sparsity score

For multimodal data, a specific novel multimodal iterative sparsity score is proposed to select features across the two modalities. When we have multimodal data, it is very interesting to investigate the effectiveness of multi-modality feature selection. Conventionally methods ignore the multimodal (or multi-view) information, which treat multi-modality data as traditional data. Some important information must be overlooked in the above methods. In this section, we extend the proposed feature selection method to multimodal algorithm called multimodal iterative sparsity score (MISS). Specifically, first we construct two graphs \( G_1^L \) and \( G_2^L \) using all the features on the two feature sets. And then in each iteratively constructing \( G_1^L \) and \( G_2^L \) process, we combine the all feature
graph with the iterative graph as follows:

\[ G'_1 = G_1 + \lambda G_2 \]

\[ G'_2 = G_2 + \lambda G_1 \]

where \( G'_1 \) and \( G'_2 \) are the modified graph in each iteration and \( \lambda \) is a fixed parameter for balancing the contribution between these two terms. In our classification experiment, we set \( \lambda = 0.3 \). The modified graphs can fully fuse the information in those multimodality data. Assume, one feature is assigned with high score in modality one, that means it is important in that modality. While in the other modality, it may be overlooked. The modified graph can relieve this situation.

4. Experiments

In this section, we carry out experiments on a lot of data sets to investigate our proposed iterative sparsity score algorithm comparing with several popular feature selection approaches. Clustering experiments are conducted on real world database. Further, we apply our proposed method on multi-modality Alzheimer’s disease data to verify the feature selection ability on multimodal data set.

4.1. Illustrative toy problem

In this subsection, we use iris data set from the UCI machine learning repository\(^2\). Iris consists of 50 instances from each of 3 categories of Iris. Four features are obtained from each sample (i.e. sepal length, sepal width, petal length and petal width). We denote the four features as \( F_{\text{len}}^{\text{sep}}, F_{\text{wid}}^{\text{sep}}, F_{\text{pet}}^{\text{sep}} \) and \( F_{\text{pet}}^{\text{pet}} \), respectively. Fig. 2 shows the distribution of iris data on two dimensional features. As we can see from Fig. 2, class 1 can be linearly separable from the other two categories, while class 2 and class 3 are not linearly separable from each other. The Fig. 2 also indicates that feature \( F_{\text{pet}}^{\text{pet}} \) and \( F_{\text{pet}}^{\text{pet}} \) contain more discriminative information since there existing large margin between class 1 and other two categories on these two features.

We compare our proposed iterative sparsity score method with other four filter-type feature selection approaches, which are variance, fisher score, Laplacian score and sparsity score. Only fisher score is supervised, while others are unsupervised. Variance ranks the features as \( F_{\text{pet}}^{\text{pet}}, F_{\text{pet}}^{\text{pet}}, F_{\text{pet}}^{\text{pet}}, F_{\text{pet}}^{\text{pet}} \). Fisher score sorts those features as \( F_{\text{pet}}^{\text{pet}}, F_{\text{pet}}^{\text{pet}}, F_{\text{pet}}^{\text{pet}}, F_{\text{pet}}^{\text{pet}} \). When using Laplacian score with \( k = 10 \), the four features are sorted as \( F_{\text{pet}}^{\text{pet}}, F_{\text{pet}}^{\text{pet}}, F_{\text{pet}}^{\text{pet}}, F_{\text{pet}}^{\text{pet}} \). By using sparsity score, the four features are ranked as \( F_{\text{pet}}^{\text{pet}}, F_{\text{pet}}^{\text{pet}}, F_{\text{pet}}^{\text{pet}}, F_{\text{pet}}^{\text{pet}} \). Our proposed iterative sparsity score sorts those features as \( F_{\text{pet}}^{\text{pet}}, F_{\text{pet}}^{\text{pet}}, F_{\text{pet}}^{\text{pet}}, F_{\text{pet}}^{\text{pet}} \).

4.2. Clustering

In this subsection, the proposed iterative sparsity score feature selection method is compared with other three unsupervised filter-type feature selection approaches (i.e. variance, Laplacian score and sparsity score) for clustering task. We do not apply fisher score, since fisher score is an supervised algorithm and there is no label information in the clustering experiments.

4.2.1. Data sets

We first simply introduce the data sets used later. The data sets we perform clustering experiments on are from UCI machine learning repository. They are wine, ionosphere, sonar, spectf heart disease, digits, and steel plate faults. Table 1 summarizes the characteristic of these UCI databases. As we can see from Table 1, the databases include binary class and multi-categories data with middle size of feature numbers.

4.2.2. Experimental settings

We first rank the features of each data set via Baseline, Variance, Laplacian Score, Sparsity Score and our proposed method. The clustering task with all the original data is denoted as Baseline. Then \( k \)-means clustering is performed on the reserved \( z \) features, where \( z \) varies from 1 to \( d \) and we can get \( z \) different clustering results. The parameter \( k \) is set as the number of categories of specific data set. This process is repeated 10 times and the average performance as well as the optimal number of selected features are reported.

F-Score metric \([35]\) is used to measure the clustering performance, in order to compare the obtained label of each sample with that provided by the data. Assume we have a clustering result, then \( Precision \) and \( Recall \) criteria are defined as follows:

\[
Precision = \frac{N_1}{N_1 + N_2}
\]

---

\(^2\) http://archive.ics.uci.edu/ml
Recall = \frac{N_1}{N_1 + N_3} \tag{15}

where $N_1$ is the number of sample pairs that are clustered correctly, $N_r$ is the number of sample pairs which belong to the different categories, but are clustered into the same cluster, and $N_3$ is the number of sample pairs that belong to the same class, but are assigned to different categories. After we obtain Precision and Recall, F-Score can be calculated as follows:

F-Score = \frac{2 \times \text{Precision} \times \text{Recall}}{\text{Precision} + \text{Recall}} \tag{16}

4.2.3. Experimental results

The experimental results are shown in Table 2. The best clustering results are denoted in bold font and the optimal numbers of reserved features are presented in the brackets. The parameter $k$ in Laplacian Score is fixed as 10. The $k$-means clustering initialization for each repeat is the same for different algorithms for fair comparison. And the number of clusters is set as the categories of each data set.

As we can see from Table 2, the clustering performances of our proposed iterative sparsity score are usually the best one among those of all the other methods. Specifically, different feature selection methods get similar F-Score on wine data set. Because wine dataset is a quite simple database, since it contains only 13 features and 3 classes. Even that, our proposed method achieves the best performance 0.6640 with only 1 feature.

Fig. 3 demonstrates the clustering performance with different number of features on 6 UCI data sets. Iterative sparsity score methods always achieves the best clustering results with small dimension.

4.3. Classification for multimodal ADNI data

Alzheimer’s disease (AD) is a physical disease and is the most common cause of dementia. In this section, we perform classification experiments on the Alzheimer’s Disease Neuroimaging Initiative (ADNI) database, in order to evaluate the effectiveness of our proposed feature selection method for classification tasks.

4.3.1. ADNI data

The data we used is from the Alzheimer’s Disease Neuroimaging Initiative (ADNI) \cite{27}. It contains 202 ADNI participants with corresponding baseline MRI and FDG-PET data. In particular, 51 AD patients, 99 MCI patients and 52 normal controls (NC) are included.

In our experiment, only the data of AD patients and normal controls are used for binary classification. Fig. 4 shows MRI and PET image of a subject from ADNI database. To obtain the features, the gray matter of 93 regions of interest (ROI) are extracted as features from MR images. For PET image, we first align it to its respective MR image of the same sample using a rigid transformation. And then the average intensity of each ROI in the PET image is computed as a feature. Therefore, for each sample, we totally have 93 features from the MR image and another 93 features from the PET image.

4.3.2. Experimental settings

Classification performance is assessed between patients and normal controls. The proposed feature selection method is compared with 4 existing popular feature selection algorithms, including Variance, Fisher Score, Laplacian Score and Sparsity Score. The approach using all of the features for classification is denoted as Baseline. It is worth noting that except Fisher Score, other above feature selection methods are unsupervised without using the label information provided by the data.

Before classification, we adopt feature selection approach on the two modalities of ADNI data separately. For a sample now we have two sets of features from MRI and PET image, respectively. Although there are numerous feature fusion strategies, such as Canonical Correlation Analysis (CCA), Partial Least Squares (PLS) and Multi-task Learning (MTL), we use the simplest way to concatenate the two heterogeneous features into a long vector with 186 dimensions. The same choosing feature strategy in clustering is adopted for classification experiment.

For fair comparison, we use a 10-fold cross-validation strategy to evaluate the effectiveness of our proposed method. Specifically, the whole data are equally divided into 10 subsets. For each cross-validation, the nine sample sets are used for training and the remaining data are chosen for testing. The process is independently repeated 10 times to avoid any bias introduced by randomly partitioning the dataset in cross-validation. In this experiment, we apply LIBSVM \cite{36} for classification with a RBF kernel and default parameters. The classification accuracy is used for evaluate the performance of different methods.

4.3.3. Experimental results

The classification accuracies are presented in Table 3 and the selected dimension corresponding to the best accuracy is shown in the brackets. From Table 3, it is shown that the classification accuracy is only 87.39% when using all the features, which is below that after feature selection. It indicates the effectiveness of feature selection. The performance of our proposed method outperforms other methods, except the supervised Fisher score. That is

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<tr>
<th>Table 1: Characteristics of the UCI data sets.</th>
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<td><strong>Description</strong></td>
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<td>Feature</td>
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<td>Class</td>
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<th>Table 2: Clustering performance comparisons.</th>
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<td><strong>Dataset</strong></td>
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<td>Wine</td>
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<td>Ionosphere</td>
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<td>Sonar</td>
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<td>Spectral heart disease</td>
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<td>Horse</td>
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<td>Steel plate faults</td>
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\footnote{http://www.loni.usc.edu}
Fig. 3. Clustering performance with different number of features.
probably because even our method is unsupervised, the structural information preserved by \( \ell_1 \) graph is close to the real data information. While the accuracy achieved by Sparsity Score is lower than those of Fisher Score and Laplacian Score, we guess that the features with low sparsity score induce noise when constructing the sparse graph. The best classification performance is achieved by multimodal iterative sparsity score. That is because the multimodal extension of our method can fully exploit the multimodality in the data.

5. Conclusion

In this paper, a novel iterative sparsity score algorithm and its multimodal extension are proposed for feature selection. The proposed method can evaluate the importance of features in a iterative way, so that the \( \ell_1 \) graph can be constructed more precisely. Experimental results on both conventional clustering and multimodality classification demonstrate the effectiveness of the proposed methods compared with other popular filter-type feature selection algorithms. Specifically, our proposed method achieves the best clustering results on UCI datasets. Although it is unsupervised, the classification result on ADNI database outperforms other unsupervised approaches and is comparable to that of Fisher Score, which involves the label information.

In our future work, we try to embed category information into the proposed method and want to see it may get better results than Fisher Score. Constructing \( \ell_1 \) graph in an iterative way is time-consuming especially when there are large data samples. We will design a fast algorithm to solve this problem. As we know, \( \ell_2 \) graph can also investigate some intrinsic information from data, it is interesting to combine graphs constructed via \( \ell_1 \) and \( \ell_2 \) together.

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References


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